1. Each straight line intersects the boundary curve at most two times.
2. If a rectangle has at least one of its vertical sides intersecting the boundary curve, count it as a type $X$ rectangle and record it with a corresponding rectangle on a row next to the x -axis.
3. If a rectangle has at least one of its horizontal sides intersecting the boundary curve, count it as a type Y rectangle and record it with a corresponding rectangle on a column next to the y-axis.
4. The total number of $X$ and $Y$ type rectangles are bounded by 2 M and 2 N respectively.
5. The total area of the 'error rectangles' is bounded by $2(M+N)(b-a)(d-c) /(M N)$.

